## Algebra III - Semester 1 Review

Name:
Date: ___ Hour: $\qquad$
Directions: Solve each linear programming problem. Assume $\boldsymbol{x} \geq 0$ and $\boldsymbol{y} \geq 0$.

1. Maximize $P=2 x+2 y$ with the constraints

$$
\left\{\begin{array}{c}
x+2 y \leq 14 \\
5 x+2 y \leq 30
\end{array}\right.
$$

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2. Minimize $P=6 x+3 y$ with the constraints

$$
\left\{\begin{array}{c}
5 x+2 y \geq 20 \\
x+y \geq 7 \\
x+2 y \geq 10 \\
x \leq 15, y \leq 15
\end{array}\right.
$$

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3. Lisa has an online jewelry shop where she sells earrings and necklaces. She sells earrings for $\$ 30$ and necklaces for $\$ 40$. It takes 30 minutes to make a pair of earrings and 1 hour to make a necklace, and, since Lisa is a math tutor, she only has 10 hours a week to make jewelry. In addition, she only has enough materials to make 15 total jewelry items per week. She makes a profit of $\$ 15$ on each pair of earrings and $\$ 20$ on each necklace. How many pairs of earrings and necklaces should Lisa make each week in order to maximize her profit, assuming she sells all her jewelry?

4. A farmer has 10 acres to plant in wheat and rye. He has to plant at least 7 acres. However, he has only $\$ 1200$ to spend and each acre of wheat costs $\$ 200$ to plant and each acre of rye costs $\$ 100$ to plant. Moreover, the farmer has to get the planting done in 12 hours and it takes an hour to plant an acre of wheat and 2 hours to plant an acre of rye. If the profit is $\$ 500$ per acre of wheat and $\$ 300$ per acre of rye how many acres of each should be planted to maximize profits?

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5. a. Write a matrix $H$ to represent the data in the table below.
b. Find element $h_{23}$. What does this element represent?

Technology in Public Schools (millions)

| Type of <br> School | Videodisc <br> Players | Modems | Networks | CD-ROMs |
| :---: | :---: | :---: | :---: | :---: |
| Elementary | 25.9 | 35.1 | 26.4 | 37.9 |
| Junior High | 9.2 | 11.0 | 9.0 | 11.0 |
| Senior High | 10.7 | 14.5 | 12.9 | 14.0 |

Source: Quality Education Data
6. a. Using the data table above, create another matrix where the rows represent types of technology and columns represent type of school.
b. What are the dimensions of the new matrix?
c. Find the element $h_{23}$. What does this element represent?

